# Problem A. Broken Keyboard

Input file: standard input
Output file: standard output

Time limit: 1 second

Memory limit: 1024 megabytes

You want to type a text consisting of n uppercase Latin letters. It seems like it should be simple, right?

But suddenly your keyboard stopped working. Only the up and down arrow keys are functioning. Among the programs installed on your computer, you found a minimalist text editor that works as follows: the cursor moves through the text with the mouse, pressing the up arrow increases the letter at the cursor position by 1 cyclically (for example, from A to B, from P to Q, and from Z to A), pressing the down arrow performs the opposite operation - it decreases the letter by 1 cyclically (from A to Z, from P to O).

You also found an arbitrary text of the same length. Now you can move through the text with the mouse and change the letters to obtain the text you need.

What is the minimum number of keyboard presses you will need? The number of mouse movements can be any.

#### Input

The first line of the input contains a single integer n — the length of the string to be changed  $(1 \le n \le 10^5)$ .

The second line consists of n uppercase Latin letters and contains the original text. The third line consists of n uppercase Latin letters and contains the text that needs to be obtained in the end.

## Output

Output a single integer — the minimum number of keyboard presses required to transform the original text into the one you need.

| standard input    | standard output |
|-------------------|-----------------|
| 1                 | 0               |
| 0                 |                 |
| 0                 |                 |
| 11<br>OLYMPSCHOOL | 53              |
| TOURNAMENTS       |                 |

## Problem B. Row of Columns

Input file: standard input
Output file: standard output

Time limit: 1 second

Memory limit: 1024 megabytes

n columns with the same base radius, the i-th of which has an integer positive height  $a_i$ , are arranged in a row, starting from the 1st and ending at n. If you look from the side of the n-th column, the n-th column will be completely visible, and the other columns will either be completely hidden (if they are fully covered by other columns) or partially visible.

For example, if the columns have heights 1, 4, 2, 8, 5, 7, 7 (from the first to the seventh), then the columns 7 and 4 will be visible (with heights 7 and 8 respectively), and the other columns will be covered by others. If the columns have heights 2, 8, 5, 7, 1, 4, then the columns 6, 4, and 2 will be visible (with heights 4, 7, and 8 respectively), and the other columns will be covered by others.

Given the values of  $a_i$ , determine how many columns will be visible.

#### Input

The first line of the input contains a single integer n — the number of columns ( $2 \le n \le 10^5$ ). Each of the following n lines contains a single integer  $a_i$  — the height of the column with number i ( $1 \le a_i \le 10^5$ ).

#### Output

Output a single integer — the number of columns that will be visible when viewed from the side of the n-th column.

| standard input | standard output |
|----------------|-----------------|
| 6              | 3               |
| 7              |                 |
| 10             |                 |
| 8              |                 |
| 7              |                 |
| 5              |                 |
| 7              |                 |
| 4              | 4               |
| 4              |                 |
| 3              |                 |
| 2              |                 |
| 1              |                 |

# Problem C. Segments and Subsets

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 512 mebibytes

Consider a collection of segments on a coordinate axis. The coordinates of endpoints are integers from 0 to x. There is no intersecting pair of segments: for any two segments, either one of them contains another, or they have at most one common point.

Your goal is to transform your collection of segments into just a single segment [0, x]. No other segments may remain. To achieve this, you can make moves. Each move has one of the following types:

- Select two segments that have a single common point: the right endpoint of the left segment coincides with the left endpoint of the right segment. Merge them into one segment: from leftmost to rightmost point. This move does not cost anything.
- Select one segment. Expand it to the left or to the right by 1 unit. This move costs 1 coin.

If, at some moment of time, there are two or more equal segments, only one of them remains, while the other disappear instantly.

For an initial collection of segments S, let F(S) be the minimum number of coins needed to transform it into just a single segment [0, x]. You are given a collection of n segments. Consider all its  $2^n - 1$  non-empty sub-collections, calculate F for each of them, and find the sum of these values modulo  $998\,244\,353$ .

#### Input

The first line contains an integer t ( $1 \le t \le 10^5$ ), the number of test cases. The test cases follow.

Each test case starts with a line containing two integers: the number of segments n  $(1 \le n \le 10^5)$  and the coordinate x  $(1 \le x \le 10^9)$ . The next n lines describe the segments. The i-th of these lines contains two integers  $\ell_i$  and  $r_i$ : the endpoints of the i-th segment  $(0 \le \ell_i < r_i \le x)$ .

The sum of n over all test cases does not exceed  $10^5$ .

### Output

For each test case, print a line with a single integer: the required sum modulo 998 244 353.

| standard input | standard output |
|----------------|-----------------|
| 3              | 10              |
| 2 5            | 28              |
| 1 4            | 806             |
| 2 3            |                 |
| 3 8            |                 |
| 1 3            |                 |
| 3 5            |                 |
| 5 8            |                 |
| 7 10           |                 |
| 1 5            |                 |
| 2 3            |                 |
| 3 4            |                 |
| 4 5            |                 |
| 5 10           |                 |
| 6 9            |                 |
| 7 8            |                 |

# Problem D. Sum of Characteristics

Input file: standard input
Output file: standard output

Time limit: 4 seconds Memory limit: 512 mebibytes

You are given an array a consisting of n random integers from 1 to n. For its subsegment  $[\ell, r]$ , the characteristic is the value

$$C(\ell, r) = \min_{\ell \le i < j \le r} \max(a_i + j, a_j + i).$$

Your task is to calculate

$$\sum_{\ell=1}^{n} \sum_{r=\ell+1}^{n} C(\ell, r).$$

#### Input

The first line contains an integer t ( $1 \le t \le 3 \cdot 10^5$ ), the number of test cases. The test cases follow.

The first line of each test case contains an integer n, the size of the array  $(1 \le n \le 3 \cdot 10^5)$ . The next line contains the array itself: n integers from 1 to n, picked uniformly and independently by a pseudorandom number generator.

The sum of n over all test cases does not exceed  $3 \cdot 10^5$ .

#### Output

For each test case, output a line with a single integer: the sum of characteristics over all the subsegments.

| $standard\ input$ | $standard\ output$ |
|-------------------|--------------------|
| 3                 | 4                  |
| 2                 | 72                 |
| 2 1               | 112                |
| 5                 |                    |
| 3 5 4 1 4         |                    |
| 6                 |                    |
| 1 4 6 1 6 3       |                    |

## Problem E. Random Permutation

Input file: standard input
Output file: standard output

Time limit: 5 seconds Memory limit: 512 mebibytes

You are given a permutation p consisting of n integers from 1 to n. You want to build a sequence a from p. To do that, you perform the following operation n times:

- append the minimum element of p to the end of a;
- remove one of the ends of p (either left or right).

You are given a **random** permutation p. Your task is to calculate the number of different sequences a that can be obtained in the way described above. This number can be very large, so find it modulo  $998\,244\,353$ . Two sequences are different if there is a position at which these sequences differ.

A permutation of size n is a sequence of n distinct integers from 1 to n.

#### Input

The first line contains an integer t ( $1 \le t \le 2 \cdot 10^5$ ), the number of test cases. The test cases follow.

The first line of each test case contains an integer n, the size of the permutation  $(1 \le n \le 2 \cdot 10^5)$ . The next line contains the permutation itself: n distinct integers from 1 to n. The permutation is generated using a pseudorandom number generator.

The sum of n over all test cases does not exceed  $2 \cdot 10^5$ .

#### Output

For each test case, output a line with a single integer: the required number modulo 998 244 353.

| standard input | $standard\ output$ |
|----------------|--------------------|
| 4              | 8                  |
| 5              | 7                  |
| 4 3 5 1 2      | 2                  |
| 5              | 4                  |
| 5 3 1 2 4      |                    |
| 2              |                    |
| 2 1            |                    |
| 3              |                    |
| 1 3 2          |                    |

## Problem F. Game

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 512 mebibytes

Consider an infinite coordinate axis. Flowers bloom in points with coordinates 1, 2, ..., n. The flower at point i has attractiveness  $a_i$ .

Two players are playing a game. The first player starts at point 1. Then they proceed as follows:

- 1. The first player, who now stands at point i, picks an integer distance from  $\ell_i$  to  $r_i$ , and moves to the right by this distance.
- 2. If the first player's coordinate is more than n, then the game stops.
- 3. Otherwise, the second player moves the first player to the left by any distance from 0 to c. However, this move can not end to the left of the point i + 1.
- 4. The first player takes the flower in his current point, and game returns to step 1.

The first player wants to maximize the total attractiveness of the flowers he takes, while the second player wants to minimize it.

Your task is to calculate the final total attractiveness of the flowers the first player has gathered if both players play optimally.

#### Input

The first line contains an integer t ( $1 \le t \le 3 \cdot 10^5$ ), the number of test cases. The test cases follow.

The first line of each test case contains two integers: the number of flowers n  $(1 \le n \le 3 \cdot 10^5)$  and the limit c  $(0 \le c \le n)$ . Each of the next three lines contains n integers: these lines describe the arrays  $\ell$ , r, and a, in this order  $(1 \le \ell_i \le r_i \le n; -10^9 \le a_i \le 10^9)$ . Note that attractiveness can be negative.

The sum of n over all test cases does not exceed  $3 \cdot 10^5$ .

#### Output

For each test case, output a line with a single integer: the final total attractiveness if both players play optimally.

| standard input | $standard\ output$ |
|----------------|--------------------|
| 2              | 3                  |
| 6 2            | -9                 |
| 1 1 2 2 1 1    |                    |
| 2 1 3 2 1 1    |                    |
| 2 3 1 -1 -1 1  |                    |
| 4 4            |                    |
| 1 1 1 1        |                    |
| 2 2 1 1        |                    |
| -1 -3 -2 -4    |                    |

# Problem G. Permutation and Queries

Input file: standard input
Output file: standard output

Time limit: 5 seconds Memory limit: 512 mebibytes

You are given a permutation  $p_1, p_2, \ldots, p_n$  of size n. Calculate the value

$$f(p) = \min_{i \neq j} |i - j| \cdot |p_i - p_j|.$$

You are also given q queries. The i-th query consists of two indices  $a_i$  and  $b_i$ . You should swap the elements at these positions (swap  $p_{a_i}$  and  $p_{b_i}$ ), and then recalculate the value f(p). Note that the changes persist between queries: after i-th query, there are i swaps made.

A permutation of size n is a sequence of n distinct integers from 1 to n.

#### Input

The first line contains two integers: the permutation size n ( $2 \le n \le 10^5$ ) and the number of queries q ( $1 \le q \le 10^5$ ).

The second line describes the permutation p.

Each of the next q lines describes a query. The i-th of these lines contains two integers  $a_i$  and  $b_i$   $(1 \le a_i, b_i \le n; a_i \ne b_i)$ : the indices of elements you should swap.

#### Output

Print q + 1 lines: the value f(p) before all queries and after each of the q queries.

| $standard\ output$ |                  |
|--------------------|------------------|
| 2                  |                  |
| 1                  |                  |
| 1                  |                  |
| 1                  |                  |
| 2                  |                  |
| 1                  |                  |
|                    |                  |
|                    | 2<br>1<br>1<br>1 |

## Problem H. Make a Palindrome

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 512 mebibytes

You have a string s consisting of lowercase English letters. You want to transform it into a palindrome by performing zero or more operations. In one operation, you can swap any two characters in the string which are at distance exactly 2 from each other (in other words, there is exactly one character between them).

Determine if it is possible to transform the string s into a palindrome.

A palindrome is a string that coincides with its reversed copy.

#### Input

The first line contains an integer t  $(1 \le t \le 10^5)$ , the number of test cases. The test cases follow.

The first line of each test case contains an integer n ( $1 \le n \le 10^5$ ). The second line contains the string s of length n consisting of lowercase English letters.

The sum of n over all test cases does not exceed  $10^5$ .

#### Output

For each test case, print a line containing "YES" if it is possible to transform the given string into a palindrome by the given rules, or "NO" otherwise.

| standard input | standard output |
|----------------|-----------------|
| 8              | YES             |
| 6              | NO              |
| acbbca         | YES             |
| 6              | YES             |
| acbbac         | YES             |
| 6              | YES             |
| aaaaaa         | NO              |
| 7              | YES             |
| abcacba        |                 |
| 9              |                 |
| abcbcecea      |                 |
| 1              |                 |
| Ъ              |                 |
| 2              |                 |
| ca             |                 |
| 2              |                 |
| сс             |                 |

# Problem I. Good Subsegments

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 512 mebibytes

You are given an array a[1..n] consisting of n integers from 1 to n. A subsegment  $a[\ell..r]$  of the array is its consecutive part from position  $\ell$  to position r, inclusive.

A subsegment  $a[\ell..r]$  is k-good if the following conditions are satisfied:

- $r \ell + 1 \ge 2 \cdot k$ , so its length is at least  $2 \cdot k$ ;
- $a_{\ell} = a_{\ell+1} = a_{\ell+2} = \dots = a_{\ell+k-1}$ , so at least k of its leftmost elements are equal to each other;
- $a_r = a_{r-1} = a_{r-2} = \dots = a_{r-k+1}$ , so at least k its rightmost elements are equal to each other;
- $a_{\ell} = a_r$ , so its ends are equal.

For each k from 1 to  $\lfloor \frac{n}{2} \rfloor$ , find the number of k-good subsegments of the given array a.

#### Input

The first line contains an integer t ( $1 \le t \le 5 \cdot 10^5$ ), the number of test cases. The test cases follow.

The first line of each test case contains an integer n  $(2 \le n \le 5 \cdot 10^5)$ .

The second line consists of n integers  $a_1, a_2, \ldots, a_n$   $(1 \le a_i \le n)$ .

The sum of n over all test cases does not exceed  $5 \cdot 10^5$ .

### Output

For each test case, print a line with  $\lfloor \frac{n}{2} \rfloor$  integers: the number of k-good subsegments for each corresponding k, starting from 1.

| standard input          | $standard\ output$ |
|-------------------------|--------------------|
| 4                       | 28 11 3 0 0        |
| 10                      | 10 2 0             |
| 1 2 2 2 2 2 3 2 2 2     | 16 3 0 0           |
| 6                       | 10 1 0 0 0         |
| 1 1 1 2 1 1             |                    |
| 9                       |                    |
| 2 2 1 1 1 2 2 1 1       |                    |
| 10                      |                    |
| 3 2 3 2 4 2 10 10 10 10 |                    |

# Problem J. Funny Numbers

Input file: standard input
Output file: standard output

Time limit: 1 second

Memory limit: 1024 megabytes

A number is called *funny* if it can be represented as the sum of three consecutive non-negative integers. Given a number, determine whether it is funny or not.

#### Input

The first line of the input contains a single integer n  $(1 \le n \le 10^8)$ .

#### Output

Output 1 if n is a funny number, and 0 otherwise.

| standard input | standard output |
|----------------|-----------------|
| 2024           | 0               |
| 2022           | 1               |

## Problem K. Maximize the Minimum

Input file: standard input
Output file: standard output

Time limit: 4 seconds
Memory limit: 512 mebibytes

You have an array a of length n and an array b of length m. You can choose to remove some elements from the arrays. Removing element  $a_i$  costs  $c_i$  coins, and removing element  $b_j$  costs  $d_j$  coins. Importantly, there should be **at least one** element left in a and **at least one** left in b.

When you are done removing the elements, you compute the following value:

$$\min_{\substack{1 \le i \le n \\ 1 \le j \le m}} |a_i - b_j|.$$

You want to maximize this value. What is the maximum value you can get if you can spend at most s coins in total?

#### Input

The first line contains an integer t  $(1 \le t \le 2 \cdot 10^5)$ , the number of test cases. The test cases follow.

The first line of each test case contains integers n ( $1 \le n \le 2 \cdot 10^5$ ), m ( $1 \le m \le 2 \cdot 10^5$ ) and s ( $0 \le s \le 10^{18}$ ). The next four lines contain integer arrays a, b, c, d, in this order ( $-10^9 \le a_i, b_j \le 10^9$ ;  $1 \le c_i, d_j \le 10^{12}$ ). The arrays a and c have length n. The arrays b and d have length m.

The sum of n over all test cases does not exceed  $2 \cdot 10^5$ . The sum of m over all test cases does not exceed  $2 \cdot 10^5$ .

## Output

For each test case, print the maximum possible value you can get.

| $standard\ input$ | $standard\ output$ |
|-------------------|--------------------|
| 2                 | 14                 |
| 1 4 10            | 3                  |
| 15                |                    |
| 1 6 9 13          |                    |
| 8                 |                    |
| 3 1 2 4           |                    |
| 5 4 4             |                    |
| -1 5 3 2 -4       |                    |
| -7 8 6 2          |                    |
| 2 3 1 1 2         |                    |
| 3 1 1 1           |                    |

# Problem L. Permutations and Cycles (Maximum Version)

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 512 mebibytes

For a given x, a permutation of size n is called *good* if for each  $1 \le i < n$  the condition  $p_i + p_{i+1} \le x$  holds. Find any good permutation with the **maximum** number of cycles.

A permutation of size n is a sequence of n distinct integers from 1 to n.

A cycle of a permutation p is a sequence of indices  $i_1, i_2, \ldots, i_k$  such that  $p_{i_1} = i_2, p_{i_2} = i_3, \ldots, p_{i_k} = i_1$ . The cycles obtained by a cyclic shifting of the sequence are considered to be the same.

#### Input

The first line contains an integer t  $(1 \le t \le 2 \cdot 10^5)$ , the number of test cases. The test cases follow.

Each test case is given on a line with two integers n ( $2 \le n \le 2 \cdot 10^5$ ) and x ( $n+1 \le x \le 2 \cdot n-1$ ). These constraints guarantee that at least one *good* permutation exists.

The sum of n over all test cases does not exceed  $2 \cdot 10^5$ .

### Output

For each test case, print two lines. The first one should contain the maximum number of cycles in a good permutation of length n. The second line should consist of n integers: the permutation itself. If multiple such permutations exist, print any one of them.

| standard input | standard output |
|----------------|-----------------|
| 3              | 2               |
| 2 3            | 1 2             |
| 3 4            | 2               |
| 3 5            | 2 1 3           |
|                | 3               |
|                | 1 2 3           |